



## INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

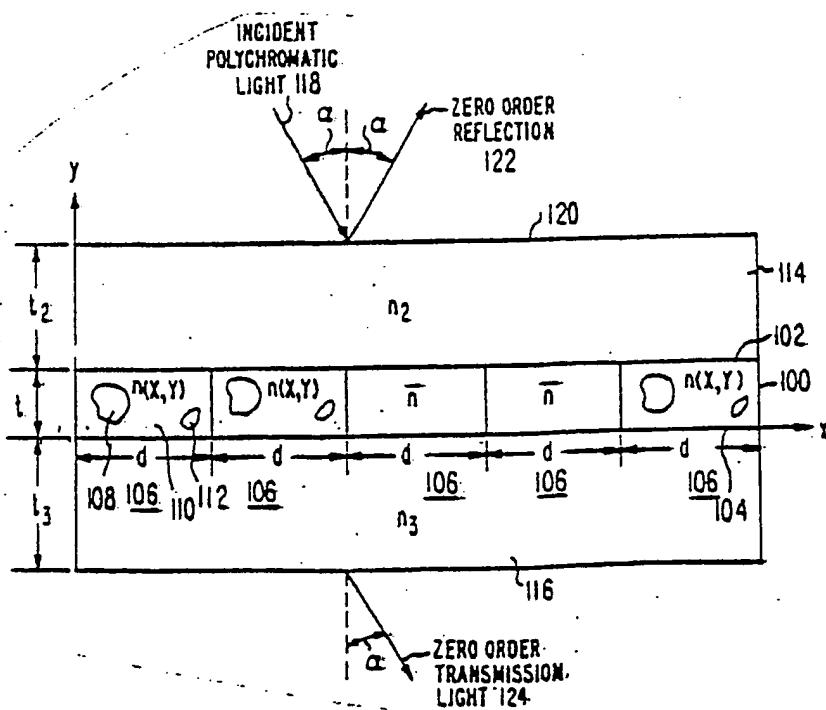
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(54) Title: DIFFRACTIVE SUBTRACTIVE COLOR FILTER RESPONSIVE TO ANGLE OF INCIDENCE OF POLYCHROMATIC ILLUMINATING LIGHT

(57) Abstract

A diffractive subtractive color filter (Fig. 1) includes a variable index-of-refraction optical medium (100) of certain minimum thickness (t) and periodicity (d) with respect to the wavelength of incident light. The filter meets certain specified constraints with respect to: (1) relative indices-of-refraction of both its internal structure and that of its surroundings (114, 116), (2) relative values of incident wavelength to periodicity and (3) the relative indices-of-refraction of the optical medium and its surroundings, and operates to produce both angularly-dependent subtractive-color filter reflection spectra and subtractive-color filter transmission spectra in accordance with its physical parameters. Such filters are suitable for use as authenticating devices for sheet-material authenticated items.



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-1-

1

DIFFRACTIVE SUBTRACTIVE COLOR FILTER  
RESPONSIVE TO ANGLE OF INCIDENCE OF  
POLYCHROMATIC ILLUMINATING LIGHT

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This invention relates to diffractive subtractive color filters and, more specifically, to a new type of diffractive subtractive color filter which is particularly suitable for use as an authenticating device for an authenticated item comprised of sheet material.

10

Reference is made to U.S. Patent No. 3,957,354, which issued May 18, 1976 to Knop, and is assigned to the same assignee as the present invention. This patent, which relates to a diffractive subtractive color filtering technique, employs a diffracting phase medium (which may be transmissive or reflective) illuminated by polychromatic (e.g., white) light to segregate zero diffraction order output light from higher diffraction order output light. The zero diffraction order output light is subtractively color filtered to possess color characteristics determined by such parameters as the effective optical peak amplitude and the waveform profile of spatially distributed diffraction elements of the diffracting phase medium. The aggregate of the higher diffraction orders possess color characteristics which are the complement of the zero diffraction order. As discussed in this patent, diffractive subtractive color filters, which employ no dyes, may be used in the projection of color pictures. In this case, the zero diffraction order may be projected through an aperture which is sufficiently wide to admit the zero diffraction order, but not wide enough to admit any of the higher diffraction orders.

15

Reference is further made to co-pending U.S. Patent application serial No. 235,970, which was filed by Webster et al on February 19, 1981, and is assigned to the same assignee as the present invention. This patent application describes a sheet-material authenticating item with a reflective diffractive authenticating device, which



1 uses a reflective (rather than transmissive) diffractive color filter, of a type disclosed in U.S. Patent No. 3,957,354, to authenticate various items of sheet-materials which are subject to counterfeiting. Such 5 items include bank notes and other valuable documents, credit cards, passports, security passes and phonograph records for their covers, for example. Such an authenticating device prevents would-be counterfeiters from employing advanced photocopying machines for the 10 color copying of documents. Such color copying machines, now or at least in the near future, would be capable of providing such high fidelity color copies that a non-expert would find it very difficult, if not 15 impossible, to discriminate between a counterfeit and a genuine article. The basic requirement for an authenticating device attached to an authenticated item is that the authenticating device possess a distinctive characteristic that is not capable of being photocopied. 20 Additional requirements are that the distinctive characteristic be easily recognized by the man-in-the-street; that the technical sophistication and capital cost needed to fabricate authenticating devices be high, and that the variable cost per unit plus the 25 amortization of the high capital cost per unit be sufficiently low as not to be an impediment to its use.

As brought out in the aforesaid co-pending patent application, a reflective diffractive subtractive color filter meets all these requirements. Such a filter 30 has the characteristic of producing angularly-separated reflected diffraction orders of different colors in response to the illumination thereof by polychromatic light. Such a characteristic cannot be copied by a photocopying machine. By merely tilting the authenticated item, angular separation between the zero and first orders 35 and the angular width of each order are sufficiently large to provide a difference in color hue that is easily discernable by a man-in-the-street. Furthermore, such a diffractive structure requires high sophistication and a



1 high capital cost to make an original embossing master,  
which then can be replicated by embossing the diffractive  
structure in plastic film. This replication technique  
permits low unit cost to be achieved in the fabrication of  
5 reflective diffractive authenticating devices.

10 The present invention is directed to a new type  
of diffractive subtractive color filter that exhibits  
unusual optical characteristics in both reflection and  
transmission. In reflection, the diffractive subtractive  
color filter of the present invention operates as a  
colored mirror, in which the color of the mirror varies  
with the viewing angle. Like any other mirror, the  
viewing angle is an angle of reflection in which the  
15 reflected light at that viewing angle depends on the light  
incident on the mirror at an angle of incidence equal to  
that angle of reflection but is totally independent of any  
light incident on the mirror at any angle of incidence  
unequal to the angle of reflection of that viewing angle.  
Therefore, by way of one example, the colored mirror of  
20 the present invention may appear as a red mirror when  
viewed at a normal angle to the surface of the filter, but  
as a green mirror when viewed at an angle of 20° with  
respect to the normal to the surface. In the special case  
25 of non-absorptive structures the color characteristics of  
this novel diffractive subtractive color filter in  
transmission are the complement of those in reflection.  
Therefore, the color characteristics in transmission also  
show an angular dependence. These angularly dependent  
30 color characteristics, in both reflection and  
transmission, are specifically determined by the  
respective values of certain physical parameters of the  
diffractive structure comprising the novel diffractive  
subtractive color filter of the present invention.  
35 Although its use is not limited thereto, the diffractive  
subtractive color filter of the present invention can be  
used to great advantage as a reflective diffractive  
authenticating device in accordance with the teaching of  
the aforesaid co-pending patent application.



-4-

1 More specifically, the present invention is  
concerned with a diffractive subtractive color filter  
responsive to polychromatic illuminating light having a  
given wavelength spectrum incident thereon for deriving  
5 reflection spectra which vary as a function of the angle  
of incidence and polarization of the illuminating light.  
The diffractive subtractive color filter also derives  
transmission spectra which are substantially (in the  
10 special case of non-absorptive structures exactly) the  
complement of the reflection spectra. Structurally, the  
filter comprises a first optical medium having a thickness  
t between two opposite faces thereof. The first optical  
15 medium has a varying index-of-refraction which divides the  
first optical medium into juxtaposed periodic diffraction  
elements of a diffractive structure having a period d  
which extends in a direction substantially parallel to the  
faces and perpendicular to a given direction. Therefore,  
20 each one of the diffraction elements extends along a  
direction substantially parallel to the faces and parallel  
to the given direction. Furthermore, the spatial  
distribution of the varying index-of-refraction within the  
volume of each diffraction element divides that  
25 diffraction element into a plurality of separate  
three-dimensional regions of certain-valued  
indices-of-refraction, which include one or more regions  
of relatively higher index-of-refraction and one or more  
regions of relatively lower index-of-refraction. Each of  
30 the regions has a specified size and shape, whereby the  
entire volume of each diffraction element has an average  
index-of-refraction  $\bar{n}$ . This array of diffracting elements  
is normally embedded between a second optical medium with  
refractive index  $n_2$  and a third optical medium with  
35 refractive index  $n_3$ .

Let us define the spectral range of interest  
extending from a minimum wavelength  $\lambda_1$  up to a maximum  
wavelength  $\lambda_2$ . This spectral range may lie in the visible  
range ( $0.4 \mu\text{m} \leq \lambda \leq 0.7 \mu\text{m}$ ) or anywhere else in the  
electromagnetic spectrum. By the term wavelength we mean



-5-

1 the free-space wavelength (it is assumed that the  
 wavelength in air is substantially the free-space  
 wavelength). The structures to be described below satisfy  
 5 the following relationships.

$$\bar{n} > \max(n_2, n_3) \quad (1)$$

$$d \max(n_2, n_3) < \lambda_2 \quad (2)$$

$$10 d(\bar{n} + 1) > \lambda_1 \quad (3)$$

$$4 \bar{n} t \geq \lambda_1 \quad (4)$$

15 where  $\max(n_2, n_3)$  is generally the larger of  $n_2$  and  $n_3$ , but, in the special case where  $n_2 = n_3$ , is  $n_2$  or  $n_3$ . The result is that the characteristics of each of the spectra depends on (1) the angle of incidence of the illuminating light, (2) the specified size and shape of each of the regions of the certain-valued relatively higher and relatively lower indices-of-refraction (which, in turn, determine the value of  $\bar{n}$ ), and (3) the respective physical 20 values of  $d$  and  $t$ .

In the drawings:

25 FIG. 1 is a diagram illustrating a generalized embodiment of a diffractive structure incorporating the principles of the present invention;

FIG. 2 illustrates one specific, geometrically simple, example of the diffractive structure shown generally in FIG. 1;

30 FIG. 3 is a flow chart showing the steps for fabricating a first practical example of the diffractive structure shown generally in FIG. 1;

FIG. 3a illustrates a first modification of the example of FIG. 3;

35 FIG. 3b illustrates, in idealized form, the diffractive structures of FIGS. 3 and 3a, having a predetermined set of relative parameter values, and FIG. 3c, 3d and 3e illustrate, respectively, the zero-order reflection spectra of the structure shown in FIG. 3b for



1 polychromatic illuminating light at angles of incidence of  
0°, 20° and 40°;

5 FIG. 4 illustrates a second modification of a  
diffractive structure fabricated by the method shown in  
FIG. 3;

10 FIG. 4a illustrates, in idealized form, the  
diffractive structure of FIG. 4, having a predetermined  
set of relative parameter values, and FIGS. 4b and 4c  
illustrate, respectively, the zero-order reflection  
spectra of the structure shown in FIG. 4a for  
polychromatic illuminating light at angles of incidence of  
0° and 30°;

15 FIG. 5 illustrates a third modification of a  
diffractive structure fabricated by the method of FIG. 3;

20 FIG. 5a illustrates, in idealized form, the  
diffractive structure of FIG. 5 having a predetermined set  
of relative parameter values, and FIGS. 5b and 5c  
illustrate, respectively, the zero-order reflection  
spectra of the structure shown in FIG. 5a for  
polychromatic illuminating light at angles of incidence of  
0° and 20°;

25 FIGS. 6a and 6b, respectively, illustrate the  
zero-order spectra of an experimental filter, which was  
actually constructed and had a diffractive structure  
similar to that shown in FIG. 4, for visible polychromatic  
illuminating light at angles of incidence of 0° and 30°;

30 FIG. 7 illustrates a fourth modification of a  
diffractive structure fabricated by the method shown in  
FIG. 3; and

35 FIGS. 8 and 9 illustrate uses of a diffractive  
subtractive color filter incorporating the present  
invention as an authenticating device for an authenticated  
item.

35 The term "light," as used herein, includes  
visible light having a wavelength spectrum of 0.4 - 0.7  
micrometers, ultraviolet light having wavelength spectrum  
below 0.4 micrometer, and infra-red light having a  
wavelength spectrum above 0.7 micrometer. However,



1 although not limited thereto, the present invention is  
particularly suitable for use with diffuse polychromatic  
visible (e.g. white) light incident on a diffractive  
5 subtractive color filter incorporating the present  
invention that is simultaneously incident on the filter at  
all angles of incidence between 0° and 90°.

10 It is known that obliquely incident light is  
refracted when it passes the interface between two optical  
such refraction effects need not be considered in order to  
understand the principles of the present invention.  
Therefore, for the sake of clarity in describing the  
15 present invention, refraction effects have been ignored.

20 The expression "free space wavelength," as used  
herein, is meant to include the wavelength in air or the  
like, as well as a vacuum, since, compared to the  
index-of-refraction of the materials comprising the filter  
itself, the difference between the index-of-refraction of  
the air and that of a vacuum is negligible.

25 Referring to FIG. 1, there is shown a first  
optical medium 100 having a thickness  $t$  between two  
opposite faces 102 and 104 thereof. As shown in FIG. 1,  
the thickness  $t$  extends in a vertical Y direction, and the  
faces 102 and 104 extend in a horizontal X direction and  
in a Z direction (not shown) perpendicular to the plane of  
the paper. Optical medium 100 has a varying  
30 index-of-refraction which divides it into juxtaposed  
periodic diffraction elements 106 having a period  $d$  which  
extends in the X direction. This results in each one of  
diffraction elements 106 extending along the Z direction  
(not shown), perpendicular to the plane of the paper. The  
35 spatial distribution  $n(x, y)$  of the varying  
index-of-refraction within the volume of each diffraction  
element 106 divides that diffraction element 106 into a  
plurality of separate three-dimensional regions (e.g.,  
regions 108, 110 and 112) of certain-valued relatively  
higher and relatively lower indices-of-refraction. As  
shown in FIG. 1, each of these regions has a specified



-8-

1 size and shape. This results in the entire value of each  
2 diffraction element 106 having an average  
3 index-of-refraction  $\bar{n}$ . In FIG. 1, the fine-structure  
4 regions 108, 110 and 112 are illustrated for the first,  
5 second and last diffraction elements 106, while only the  
6 average index-of-refraction  $\bar{n}$  is indicated for the third  
7 and fourth diffraction elements 106. It should be  
8 understood, however, that both the fine-structure and the  
9 average index-of-refraction  $\bar{n}$  of all the diffraction  
10 elements 106, FIG. 1 are similar.

15 Contacting face 102 is second optical medium 114  
16 having a thickness  $t_2$  in the Y direction and having an  
17 index-of-refraction  $n_2$ . Contacting face 104 is third  
18 optical medium 116 having a thickness  $t_3$  in the Y  
19 direction and having an index-of-refraction  $n_3$ .

20 Assuming that the amount of any absorption  
21 within the diffractive subtractive color filter of FIG. 1  
22 is negligible, a first portion of polychromatic  
23 illuminating light 118 incident on top surface 120 of  
24 second optical medium 114 at an angle  $\alpha$  with respect to  
25 the normal ultimately gives rise to zero-order reflection  
26 output light 122 at an angle of reflection  $\alpha$  with respect  
27 to the normal. A second portion of polychromatic light  
28 118 incident on top surface 120 at an angle  $\alpha$  with respect  
29 to the normal ultimately gives rise to zero-order  
30 transmission light 124 emerging from the bottom surface of  
31 third optical medium 116 at an angle  $\alpha$  with respect to the  
32 normal.

33 The polarization and color characteristics of  
34 the spectra of zero-order reflection light 122 for each  
35 angle of reflection depend on the wavelength spectrum and  
the physical parameters of the diffractive subtractive  
color filter shown in FIG. 1. These physical parameters  
include the respective values of the period  $d$  of the  
diffraction elements 106 and the thickness  $t$  of first  
optical medium 100; the respective values of the  
index-of-refraction  $n_2$  of second optical medium 114 and  $n_3$



1 of third optical medium 116, and the respective values of  
variable index-of-refraction  $n(x, y)$  as a function of  
spatial distribution within the volume of each diffractive  
5 element 106, which respective values define the size and  
shape of each of regions 108, 110 and 112 and the average  
index-of-refraction  $\bar{n}$  of each diffraction element 106.  
These same factors determine the color and polarization  
10 characteristics of the spectra of zero-order transmission  
light 124 emerging at an angle  $\alpha$ , relative to the normal  
since transmission light 124 exhibits color  
characteristics which in the special case of  
non-absorptive structures are the complement of zero-order  
reflection light 122.

15 It is known that light is an electromagnetic  
wave and that the properties of electromagnetic waves are  
defined by Maxwell's equations. It is also known that  
where the period  $d$  of a diffractive structure is much  
smaller than the wavelength of incident light, the  
20 incident light is not affected by (i.e., does not see) the  
diffractive structure. It is also known that where the  
period  $d$  of the diffractive structure is substantially  
larger than the wavelength of incident light, the  
diffractive properties of the diffractive structure can be  
25 determined, with negligible error, without resorting to  
Maxwell's equations by utilizing the simplifying  
approximations provided by Kirchhoff-Huygens wave theory.  
However, as is the case in the present invention, when the  
behavior of a diffractive structure depends upon  
30 illuminating light having a wavelength spectrum that  
comprises wavelengths in the general neighborhood of the  
period  $d$  of the diffractive structure, it is essential  
that Maxwell's equations be utilized to determine the  
properties of the diffractive structure.

35 Relationship (1) given previously is:  
 $\bar{n} > \max(n_2, n_3)$ . This implies that the value of the  
average index-of-refraction  $\bar{n}$  of the diffractive structure  
formed by first optical medium 100 in FIG. 1 is larger  
than the value of the index-of-refraction  $n_2$  of the second



1        optical medium 114 contacting upper face 102 of first  
 optical medium 100 and also is larger than the value of  
 the index-of-refraction  $n_3$  of third optical medium 116  
 contacting lower face 104 of optical medium 100.

5        Relationship (2) states:

$$d \max(n_2, n_3) < \lambda \quad (2)$$

10       The effect of this constraint is to prevent (at least in a  
 portion of the spectral range of interest and with the  
 viewing angle being equal to an angle of incidence  $\alpha = 0$ )  
 any diffraction orders other than zero order that may have  
 been generated with first optical medium 100, from ever  
 emerging into the ambient. Thus, all the reflected light  
 15       and all the transmitted light that emerges into the  
 ambient that has been ultimately derived from  
 polychromatic light 118 having normal incidence (i.e.,  
 $\alpha = 0$ ) is comprised solely of zero-order reflection light  
 122 and zero-order transmission light 124

20       Relationship (3) states:

$$d(\bar{n} + 1) > \lambda_1 \quad (3)$$

25       Since in first optical medium 100, the average  
 index-of-refraction  $\bar{n}$  is large relative to the  
 substantially unity index-of-refraction of the ambient,  
 the wavelength of light within first optical medium 100  
 will be shorter than the corresponding free-space  
 wavelength in the ambient. Relationship (3) implies that  
 30       at least for an angle of incidence  $\alpha$  approaching  $90^\circ$   
 within first optical medium 100, the zero diffraction  
 order and at least one first diffraction order can both  
 propagate. Further, in order for both relationship (2)  
 and relationship (3) to be true, the respective values of  
 35       the free-space  $\lambda$  and  $d$  must be fairly close to one  
 another. Therefore, it is necessary to make use of  
 Maxwell's equations to predict the optical properties of  
 the diffractive subtractive color filter shown in FIG. 1.

Relationship (4) states:



-11-

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$$t \geq \frac{\lambda}{4n}$$

(4)

Relationship (4) signifies that first optical medium 100 is of sufficient thickness  $t$  to ensure that constructive and destructive interference (due to different path lengths) occurs at some wavelengths of the wavelength spectrum of the polychromatic light between those rays of light reflected from face 102 and those rays of light reflected from face 104 which ultimately combine to form zero-order reflection light 122.

The filtering characteristics of a diffractive subtractive color filter that conforms with all the above constraints depends on the specific values of its physical parameters such as  $n_2$ ,  $n_3$ , the function  $n(x, y)$ , which determines the size and shape of each of regions 108, 110 and 112, and the physical values of  $t$  and  $d$ . In order to design a particular filter, Maxwell's equations must be solved for a selected set of these physical parameters at various relative wavelengths within a relative wavelength spectrum of  $\lambda/d$ . In practice, it takes a computer to perform the many calculations required to solve, by numerical analysis, Maxwell's equations for any particular set of physical parameters. Alternatively, a filter having specific values of its physical parameters can be constructed, and its reflective spectra characteristics can be measured.

As shown in FIG. 1, second optical medium 114 and third optical medium 116 comprise separate layers of material having respective thicknesses  $t_2$  and  $t_3$  which usually are much larger than the thickness  $t$  of first optical medium 100. The respective indices  $n_2$  and  $n_3$  of the material forming second optical medium 114 and third optical medium 116, while being smaller than the value of the average index-of-refraction  $\bar{n}$ , are generally greater than the substantially unity index-of-refraction of the ambient. However, this is not essential. In principle, at least, second optical medium 114 and/or third medium 116 could be either air or a vacuum. In this special



1 case, polychromatic light 118 could be incident directly  
on face 102, so that zero-order reflection light 122  
and/or zero-order transmission 124 would emerge directly  
5 from surface 102 and/or surface 104.

10 FIG. 2 shows a geometrically simple specific  
example of a diffractive subtractive color filter of the  
type shown in generalized form in FIG. 1. In the specific  
example of FIG. 2, first optical medium 100 is comprised  
15 of periodically spaced rectangular regions 200 composed of  
a material having an index-of-refraction  $n_1 = 3$ . These  
relatively high index-of-refraction regions 200 are  
separated by rectangular regions 202 having a relatively  
low index-of-refraction  $n_0 = 1.5$ . Both second optical  
20 medium 114 and third optical medium 116 have  
indices-of-refraction  $n_2$  and  $n_3$  also equal to 1.5. The  
thickness  $t$  of first optical medium 100 (which is the  
height of both rectangular regions 200 and 202) has the  
relative value of 0.625  $d$ , where  $d$  is the spatial period  
25 of the diffractive elements formed by each pair of  
adjacent regions 200 and 202. The width  $w$  of each higher  
index-of-refraction rectangular region 200 has a relative  
value equal to 0.125  $d$ . Therefore, the width of each  
lower rectangular region 202 has a relative value equal to  
0.875  $d$ .

30 The optical mediums 114 and 116 have thicknesses  
 $t_2$  and  $t_3$  which are very much larger than the spatial  
period  $d$  of first optical medium 100. By way of example,  
the value of the thickness  $t_2$  may have a relative value of  
35 37.5  $d$ , whereas the thickness  $t_3$  is assumed to be so large  
as to extend indefinitely.

35 From a theoretical standpoint, the embedded  
laminated grating shown in FIG. 2 is probably the  
geometrically simplest structure which yields the  
angular-dependent reflective spectra discussed above in  
connection with FIG. 1. In order to test the validity of  
the assumptions on which the present invention is based,  
the respective spectra of the zero-order reflected light,  
for the particular implementation shown in FIG. 2, were



1 calculated on a computer for each of two angles of  
incidence. More specifically, the computer solved  
Maxwell's equations for each of four different cases,  
assuming in each case that wavelength spectrum  $\lambda/d$   
5 polychromatic light extended over a relative range of  
values of  $\lambda/d$  from 1 to 2.4. The four cases were (1) an  
angle of incidence (with respect to the normal) of  $0^\circ$  with  
the electric E vector of the incident light assumed to be  
10 polarized parallel to the line direction of the grating  
(which, in FIG. 2, is in a direction perpendicular to the  
paper); (2) an angle of incidence of  $0^\circ$  (with respect to  
the normal) with the magnetic vector H of the incident  
light assumed to be polarized parallel to the line  
direction of the grating; (3) an angle of incidence of  $20^\circ$   
15 with the electric vector E of the incident light assumed  
to be polarized parallel to the line direction grating,  
and (4) at an angle of incidence of  $20^\circ$  with the magnetic  
vector H of the incident light assumed to be polarized  
parallel to the line direction of the grating. The  
20 respective solutions of Maxwell's equation, in each of  
these four cases, for a structure having the physical  
parameters of FIG. 2, showed that both the electric and  
magnetic polarization zero-order reflection spectra are  
angularly dependent. Each of these reflection spectra is  
25 attained by plotting the percentage of zero-order  
reflection light as a function of  $\lambda/d$  over the relative  
wavelength spectrum from 1-2.4. It was found that each of  
the two electric vector spectra exhibited one large  
reflectance peak each over a sub-interval of the  $\lambda/d$   
30 spectrum together with a plurality of much lower  
reflectance peaks over the remainder of the  $\lambda/d$  of the  
wavelength spectrum. The respective positions of  
sub-intervals of the high reflectance peaks, in terms of  
35 the values of  $\lambda/d$ ; and the shape of the high reflectance  
peaks were substantially different for the case of  $0^\circ$   
incident polychromatic light from the case of  $20^\circ$  incident  
polychromatic light. The respective H vector spectra were  
composed of only relatively low reflectance peaks.



-14-

1        However, the relative height, shape and spatial  
distribution of these peaks for the case of 0° incident  
polychromatic light were different from that of 20°  
5        incident polychromatic light. Therefore, the assumptions  
on which the present invention are based are valid.

10       Different color effects can be obtained  
depending upon the particular choice of the value of d.  
With d having a value of 0.4 micrometer ( $\mu\text{m}$ ), the color  
changes from reddish to white when the angle of incidence  
is changed from 0° to 20°. However, with a value of d  
equal to 0.32 $\mu\text{m}$ , the color change is from green to red  
when the angle of incidence changes from 0° to 20°.  
15       Further, since all the spectra contain a number of low  
reflectance detailed features, such as peaks and sharp  
band edges, these peaks and sharp band edges may be  
employed in an authenticating device for machine readable  
identification. In fact, by a proper choice of the value  
20       of d, some of the peaks or sharp end edges which occur at  
longer wavelengths can be made to occur in the infra-red,  
rather than in the visible light spectrum. Furthermore,  
the E vector and the H vector reflection spectra are very  
different from each other. This strong polarization  
dependence is also suited for machine identification, when  
25       the invention is utilized in an authenticating device of  
the type discussed above. In addition, the angular  
dependence about a tilt axis parallel to grating line  
direction is significantly different from a tilt axis  
perpendicular to grating line direction. This is another  
30       discriminant that can be used for machine identification.

35       The structure in FIG. 2 was obtained by  
selecting the two refractive indices  $n_1 = 3$  and  
 $n_3 = n_2 = 1.5$ , then optimizing the thicknesses t and the  
line width w. The thickness  $t_2$  and  $t_3$  of the bottom and  
top layers are not critical as long as they are large  
compared to d. For best visibility of the reflective  
light, the bottom layer should be terminated by strongly  
absorbing (black) material. The given values of t and w



1 in FIG. 2 are not the only choices of these parameters  
that provide good results.

5 While for an authenticating device, the  
reflective zero-order spectra are used, it should be  
understood that the transmission spectra, which are also  
produced, may be useful for other purposes.

10 The main benefit of the geometrically simple  
structure of the species as shown in FIG. 2 is that it was  
easy to calculate on a computer solving Maxwell's  
equations, in order to test the validity of the present  
invention. However, the structure of FIG. 2 would be most  
difficult (if not impossible) to physically implement in a  
real structure, at the present state of the art. FIG. 3  
15 illustrates the steps of a method for fabricating  
geometrically more complex, but more practical, species of  
the present invention that have physical structures which  
are more easily realizable.

20 FIG. 3 is a flow chart showing the successive  
method steps for fabricating a finished filter employing  
the principles of the present invention, starting with a  
thermoplastic material 300 which may have a surface relief  
pattern embossed therein by a metal embossing master 302,  
by such known techniques as casting or hot pressing. By  
25 way of example, metal master 302 is shown as having a  
rectangular waveform profile of physical depth  $a$ . The  
first step is to emboss this waveform profile into the  
upper surface of thermoplastic material 300 having an  
index-of-refraction  $n_3$ . This results in the production of  
30 relief structure 304. The second step is to deposit a  
relatively thin layer of material 306 having an  
index-of-refraction of  $n_1$  and having given thickness and  
shape characteristics on the relief surface of structure  
304. Known depositing techniques includes evaporation,  
35 sputtering (particularly ion beam sputtering), spin-on  
techniques, etc. Material 306 is selected to have an  
index-of-refraction  $n_1$  which is large relative to the  
index-of-refraction  $n_3$  of thermoplastic material 300. The  
next step is to overcoat the deposited layer 306 on the



-16-

1 relief surface of structure 304 with a material 308 having  
an index-of-refrction  $n_2$ , which is relatively low compared  
with the index-of-refraction  $n_1$  of deposited layer 306.  
5 This results in a finished filter comprised of a first  
optical medium having a thickness  $t$  extending from the  
bottom of the troughs of the surface relief waveform  
profile in thermoplastic structure 304 to the top of the  
10 deposited layer 306 overlying the crests of this waveform  
profile. The first optical medium in FIG. 3 comprises  
those regions of thermoplastic structure 304 forming the  
crests of the waveform profile (index-of-refraction  $n_3$ ),  
all regions of deposited layer 306 (index-of-refraction  
15  $n_1$ ) and those portions of the troughs of this surface  
relief waveform profile which are not already filled by  
deposited layer 306 but are filled by overcoat material  
308 (index-of-refraction  $n_2$ ). In order to meet the  
constraints of the present invention, it is necessary that  
the average index-of-refraction  $\bar{n}$  of all the regions of  
20 which the first optical medium of the finished filter is  
comprised be larger than the value of either  $n_2$  or  $n_3$ .  
The second optical medium is comprised of the remainder of  
25 overcoat 308 which lies above surface relief structure 304  
and the third optical medium is comprised of the remainder  
of thermoplastic material 300 which lies below surface  
relief structure 304.

In FIG. 3, the thickness  $c$  of deposited layer  
306 happens to be smaller than the physical depth  $a$  of the  
30 embossed rectangular waveform grating. This is not  
essential. The thickness  $c$  of the deposited layer 306 may  
be larger than the depth  $a$  of the embossed rectangular  
waveform grating. In this latter case, the configuration  
of the finished filter in FIG. 3 would have the appearance  
shown in FIG. 3a, rather than that of the finished filter  
35 actually shown in FIG. 3.

FIG. 3b, in idealized form, shows a particular  
example of the species of the present invention  
represented by the finished filters of FIGS. 3 and 3a. As  
indicated in FIG. 3b, the relatively high



1 index-of-refraction of  $n_1$  of the deposited layer 306 is  
2 equal to 3; the relatively low indices-of-refraction of  $n_2$   
3 and  $n_3$  are both 1.5; the rectangular waveform period  $d$  has  
4 a 50% aspect ratio or duty-cycle (i.e., it is a square  
5 wave); the thickness  $c$  of deposited layer 306 has the  
10 relative value 0.22  $d$  and the distance between the top of  
the deposited layer 306 lying within a trough of the  
waveform and the bottom of deposited layer 306 lying above  
a crest of the deposited waveform has a relative value  
15 0.055  $d$ . Therefore, the depth  $a$  of the square-wave  
profile is 0.275  $d$  (the sum of 0.22  $d$  and 0.055  $d$ ). A  
computer programmed to solve Maxwell's equations for the  
particular configuration and values of parameters shown in  
FIG. 3b, calculated the zero-order reflection spectra  
15 shown in FIGS. 3c, 3d and 3e for various angles of  
incidence of polychromatic light over wavelength spectrum  
extending over a relative range of values  $\lambda/d$  from 1-2.5  
FIG. 3c shows both the E vector zero-order reflection  
20 spectrum and the H vector reflection spectrum for an angle  
of incidence of  $0^\circ$  with respect to the normal, while,  
FIGS. 3d and 3e show these reflection spectra for  $20^\circ$  and  
 $40^\circ$ , respectively, relative to the normal. As shown in  
FIG. 3c, at zero angle of incidence, the zero-order  
25 reflection spectrum for the E vector exhibits a large  
single peak. The position of the sub-interval of the  
relative wavelength spectrum at which this single peak  
appears is in accordance with relationship 4, discussed  
above. Specifically, the peak only occurs over a  
30 sub-interval of relative wavelengths  $\lambda/d$  which lie in the  
spectral range of interest  $\lambda_1 < \lambda < \lambda_2$  substantially  
equal to the maximum value of  $n_2$  or  $n_3$  (which in the case  
of FIG. 3b is 1.5). As stated earlier in connection of  
FIG. 2, the H vector polarization in each of FIGS. 3c, 3d  
35 and 3e contributes relatively little to the overall  
reflectance, but contains features, such as narrow, sharp  
peaks suitable for a machine identification.

More generally, the width of the single large  
peak at  $0^\circ$  (such as the large peak in FIG. 3c) increases



-18-

1 with increasing refractive index of the deposition  
material  $n_1$  and increasing deposition thickness  $c$ . A peak  
reflectance close to 100% can usually be obtained for any  
5 given type of grating profile by tuning its depth value,  
and/or its deposition thickness value. As shown in FIG.  
3c, the large peak of the E vector polarization meets all  
the above criteria. In addition, the E vector  
10 polarization shows a relatively weak reflection peak at a  
value of  $\lambda/d$  in the vicinity of unity and the H vector  
polarization shows a relatively sharp reflection peak at a  
value of  $\lambda/d$  in the vicinity of 1.52.

As indicated in FIGS. 3d and 3e, the reflection  
spectrum splits into two peaks moving symmetrically  
15 towards shorter and higher wavelengths respectively for  
angles of incidence which are oblique with respect to an  
axis (perpendicular to the plane of the paper) parallel to  
the grating lines. The amount of wavelength shift from  
the original position at  $\alpha = 0^\circ$  is of the order of  $da$ .  
However, at oblique angles with respect to an axis  
20 perpendicular to the grating lines, a much weaker shift  
towards shorter wavelengths results with no associated  
peak splitting. This weaker shift is similar to the  $\cos \alpha$   
dependent shift observed in conventional interference  
25 filter structures.

By a proper choice of the grating period  $d$ , the  
peak for  $\alpha = 0$  can be placed in the red. Then, the  
sequence is green, then blue for typical shifts to  
30  $\alpha = 15^\circ$ , then  $30^\circ$  (parallel to the grating lines).  
However, if the grating period  $d$  is chosen so that, at  
 $\alpha = 0$ , the peak is located in the green, a typical shift  
produces magenta. Finally, if the grating period  $d$  is  
35 chosen so that, at  $\alpha = 0$ , the peak is located in the blue,  
a typical shift causes the color changes to green and then  
to red. This description of color change is somewhat  
simplified, since the particular structure, such as the  
particular structure shown in FIG. 3b, exhibits its own  
specific spectral signature (which includes, in the case



1 of FIG. 3b, the effect of the middle-sized additional E  
and H vector polarization peaks shown in FIGS. 3c and 3d).

5 Typical values of the grating period  $d$  are from  
0.1 to 0.45  $\mu\text{m}$  and typical grating depths  $a$  are from 0.1  
to 0.2  $\mu\text{m}$ , when  $\lambda$  is in the visible wavelength spectrum of  
0.4-0.7  $\mu\text{m}$ . The refraction index of the deposition  
material is usually in the range from 1.7-5. In practice,  
10 the index-of-refraction  $n_1$  depends on  $\lambda$  and may be complex  
(for absorptive materials), thus introducing a further  
variability in design of the filter.

15 In FIG. 3, it is assumed that deposition takes  
places perfectly normal to the surface of the relief  
structure, so that the thickness of deposition on all the  
bottoms and on all the tops of the rectangular waveform  
profile are all equal to one another. In practice, such  
perfect deposition can only be approached, but not  
reached, by practical deposition techniques, such as  
10 evaporation or ion beam sputtering, directed normal to the  
surface of the relief structure. The result is that, in  
practice, the method of FIG. 3 tends to result in a  
finished filter having a configuration that looks more  
like FIG. 4, than either like FIG. 3 or FIG. 3a. The main  
difference between the configuration of FIG. 4 and those  
20 of FIGS. 3 and 3a is that the thickness of deposited  
material 306 overlying the troughs of the rectangular  
waveform relief structure 304 is substantially larger than  
the thickness overlying the crests of this rectangular  
waveform profile.

25 FIG. 4a shows, in idealized form, a specific  
example of a configuration which approximates the  
configuration of FIG. 4. In FIG. 4a, the value of  
relatively high index-of-refraction  $n_1$  of deposited  
material 306 is 2.3 and the indices-of-refraction  $n_2$  and  
30  $n_3$  of structure 304 and overcoat 308 are 1.5. As  
indicated in FIG. 4a, the boundary between structure 304  
and deposited layer 306 forms a square-wave profile having  
a period  $d$  and a relatively high amplitude of 0.3d. The  
35 boundary between overcoat 308 and deposited layer 306



-20-

1 forms a square-wave profile having a period  $d$  and a  
5 relatively low amplitude of  $0.1 d$ . Further, the troughs  
5 of this relatively low amplitude square-wave are situated  
at a distance of  $0.1 d$  above the crests of the relatively  
high amplitude square-wave. Therefore, in the case of  
FIG. 4a, the overall thickness  $t$  of the first optical  
medium is  $0.5 d$ .

10 FIGS. 4b and 4c, respectively, show the  
zero-order reflection spectrum for angles of incidence and  
of  $0^\circ$  and  $30^\circ$ , computed by solving Maxwell's equations for  
a filter having the configuration and physical parameters  
shown in FIG. 4a.. The similarities and differences  
between the zero-order reflection spectra shown in FIGS.  
15 4b and 4c, on one hand, and those shown in FIGS. 3c, 3d  
and 3e, on the other hand, should be noted. More  
specifically, the main feature, shown in FIG. 4b, is that,  
20 for  $0^\circ$  the strong E vector has a reflection peak relative  
value for  $\lambda$  of about  $1.8 d$ . As shown in FIG. 4c, for  $30^\circ$   
incidence, this peak splits into two peaks at a relative  
value of  $\lambda$  equal to approximately  $1.38 d$  and approximately  
25  $2.25 d$ . This is in agreement with the general principles  
discussed above in connection of FIGS. 3c, 3d and 3e. In  
addition, when the angle of incidence is  $30^\circ$ , a third peak  
in the E vector polarization spectrum is observed at a  
relative value of  $\lambda$  of about  $1.08 d$ , as shown in FIG. 4c.  
30 The H vector polarization spectrum for an angle of  
incidence of  $0^\circ$ , shown in FIG. 4b, is almost featureless.  
However, at an angle of incidence of  $30^\circ$ , as shown in FIG.  
35 4c, a complicated spectrum with several sharp resonances  
develops. It is obvious that these sharp peaks are  
ideally suited for machine identification.

35 The deposition of the deposited layer 306 need  
not be made normal to the relief surface of structure 304.  
FIG. 5 illustrates a configuration of the finished filter  
in which the layer 306 is deposited at a relatively large  
oblique angle (i.e., about  $45^\circ$ ) with respect to the relief  
surface of structure 304. Such an angular deposition may  
be accomplished by evaporation or ion beam sputtering from



1 an angularly displaced source. FIG. 5a shows, in  
idealized form, a specific example of the structure shown  
in FIG. 5. In FIG. 5a, the relatively high  
5 index-of-refraction  $n_1$  of deposited material 306 is 3 and  
the respective indices-of-refraction  $n_2$  and  $n_3$  of  
structure 304 and overcoat 308 are 1.5. In FIG. 5a, an  
10 L-shaped deposit of material 306 occurs periodically, with  
a period  $d$ , at a spacing therebetween of 0.5  $d$ . The width  
and height of the horizontal leg of each L-shaped deposit  
of material 306 are 0.5  $d$  and 0.25  $d$ , respectively. The  
width and height of the vertical leg of each L-shaped  
deposit of material 306 are 0.18  $d$  and 0.2  $d$ ,  
15 respectively. The dimensions shown in FIG. 5a approximate  
those which would be obtained using the method of FIG. 3,  
with an angle of evaporation for deposited material 306 of  
about 35°.

20 One of the benefits of the configuration shown  
in FIGS. 5 and 5a, when employed in an authenticating  
device, is that it belongs to a class, along with the  
configuration of FIG. 3, of particularly secure structures  
where each individual grating line is fully encapsulated  
by the host material. This encapsulation prevents the  
possibility that deposited layer might be peeled off to  
25 reveal the physical structure of the grating.

30 FIGS. 5b and 5c, respectively, show the  
zero-order reflection spectra for 0° and for 20° of a  
filter having the physical parameters of the configuration  
shown in FIG. 5a, as calculated from Maxwell's equations  
by a computer. As shown in FIG. 5b, the calculated E  
vector polarization spectrum for 0° has bandpass  
characteristic with very sharp edges, suitable to produce  
good colors. The H vector polarization is characterized  
35 by two sharp peaks. As shown in FIG. 5c, at 20°, the two  
shifted peaks, at relative values of  $\lambda$  about equal to 1.6  
 $d$  and about 2.3  $d$  have very much reduced intensity and do  
not produce a strong color effect. While this reduced  
intensity is in contrast to the previous examples, a  
useful application of this reduced intensity property



-22-

1 would be to put printed information on the back side of a  
structure which would not be visible for small viewing  
angles, near  $0^\circ$ , but could be seen and read at larger  
angles, near  $20^\circ$ .  
5

Numerous structures have been fabricated.  
Mainly these structures had the configurations shown in  
FIG. 3, FIG. 3a and FIG. 4. One such structure, which had  
a configuration shown in FIG. 4 (or approximately in FIG.  
10 4a) was made by first forming a square-wave surface relief  
structure ( $d = 0.38 \mu\text{m}$ , and  $= 0.12 \mu\text{m}$ ) in photoresist,  
using lithographic techniques; then depositing  
ZnS ( $t = 0.12 \mu\text{m}$ ) by vapor deposition. Finally, the device  
was covered with an ultra-violet curable epoxy. No hot  
pressing or casting technique was involved, since the  
15 fabrication was experimental and at this stage no mass  
production was intended. The physical parameters employed  
corresponded closely to those chosen for the numerical  
calculation by computer of FIG. 4a, discussed above.  
FIGS. 6a and 6b, respectively, show the zero-order  
20 reflection spectra toward  $0^\circ$  and  $30^\circ$  obtained  
experimentally from this fabricated structure. Good  
qualitative agreement is observed between the computed  
spectra shown in FIGS. 4b and 4c and the corresponding  
experimental spectra shown in FIG. 6a and 6b. All the  
25 main peaks discussed above in connection with FIGS. 4a and  
4b can be found and compared, although their intensity and  
exact positions in FIGS. 6a and 6b vary slightly.

So far in this discussion, the surface relief of  
30 structure 304 has always had a rectangular waveform  
profile. This need not be the case. FIG. 7 shows a  
species of the present invention in which the surface  
relief of structure 304 has a triangular waveform.  
Further, as shown in FIG. 7, deposited layer 306 is  
35 deposited at an oblique angle, in a manner similar to that  
discussed in connection with FIG. 5, to cover only one of  
the two exposed sides of the triangular waveform.

All of the configurations shown in FIGS. 2-7 are  
species of the filter shown in FIG. 1. These species



1 should be considered merely as illustrative examples of  
the present invention. Any other configuration, not  
shown, that conforms to the constraints discussed above in  
connection with FIG. 1, are within the purview of the  
5 present invention. Actually, an infinite number of  
different grating structures can be made, depending upon  
the particular choice of relief structure, materials,  
deposition thickness, etc.

10 All the structures described herein are  
extremely hard to counterfeit, even when it is assumed  
that the counterfeiter has large capital and technical  
resources available. This is due to at least to two  
facts. First, it is virtually impossible to investigate  
15 the geometry of a given structure by optical  
(non-destructive) means. Although it is possible to  
calculate the optical properties of a given structure, the  
inverse problem exceeds present day computing capability.  
Second, a mechanical or chemical analysis of a given  
20 structure is very hard, if not impossible, due to its  
fineness, with typical dimensions in the sub-micrometer  
range. In particular, structures, such as those shown in  
FIGS. 3, 5 and 7, are extremely difficult to separate for  
analysis because the deposition material is separated into  
25 discrete lines fully enclosed by the surrounding  
materials. Further, the first step of the method shown in  
FIG. 3 uses the surface relief pattern of a master to  
reproduce the surface relief pattern in many replicas of  
the master. Since the same master is used over and over  
30 to make replicas, the process inherently gives high  
reproducibility and cannot be easily copied, unless  
someone has access to this original master.

35 Since filter structures of the present invention  
meet all the requirements for an authenticating device of  
the type described in the aforementioned co-pending patent  
application, and, in addition, are so extremely hard to  
counterfeit, a filter structure incorporating the present  
invention is particularly suitable for use as such an  
authenticating device.



-24-

1 FIGS. 8 and 9 are similar to figures of the  
aforementioned co-pending patent application. As shown in  
FIG. 8, one or more authenticating devices, such as  
authenticating device 800, may be bonded to an  
5 authenticated item 802 comprised of sheet material, as  
discussed more fully in the aforesaid co-pending patent  
application. Authenticating device 800 may comprise a  
filter structure incorporating any of the embodiments (for  
example, the embodiment shown in Fig. 3) of the present  
10 invention. One example of such an authenticating device  
800 is shown in FIG. 9. In FIG. 9, authenticating device  
800 is comprised of a first area 900 having a dimension W  
surrounded by a second area 902. Area 900 may be made of  
a first diffractive structure incorporating the principles  
15 of the present invention which provides zero-order  
reflection light having a first color hue (such as red)  
when viewed in diffuse polychromatic light at a 0° angle  
with respect to the normal to the surface of  
authenticating device 800. Area 902 may be comprised of a  
20 second diffractive structure incorporating the principles  
of the present invention which provides zero-order  
reflection light of a second contrasting color hue (such  
as green) when viewed in diffuse polychromatic light at a  
0° angle with respect to the normal to the surface of  
25 authenticating device 800. When authenticating device 800  
(usually together with authenticating item 802) is tilted  
so that it is viewed at an oblique angle of incidence, the  
first color hue, such as red of area 900 may change to  
green, while, at the same time, the second color hue, such  
30 as green, of area 902 may change to magenta. The size of  
the dimension W of area 900 is at least sufficiently large  
so that area 902 may be easily seen at normal viewing  
distances, such as 30 centimeters.

35 In an authenticating device, as well as other  
articles of manufacture, various attributes of the present  
invention may be combined to advantage. For instance, the  
grating lines in one area such as area 900, may be  
oriented at a different angle from the grating lines of a



-25-

1 different area, such as area 902. Further, some areas  
could employ overlapping grating lines of different  
periodicities  $d$  and/or of different angular orientations.  
The fact that angular discrimination of spectra differs  
5 marked between tilting about an axis parallel to grating  
lines and tilting about an axis perpendicular to grating  
lines can be made use of in an authenticating device, as  
well as other articles of manufacture. Making use of the  
principles of the present invention, it is possible to  
10 produce character text in a manner such that it is  
discernable from the background only under certain viewing  
conditions and not for other viewing conditions. In this  
regard, a focused laser beam may be employed to write text  
characters by selectively destroying portions of a  
15 diffractive structure surface that had been fabricated in  
accordance with the principles of the present invention.

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-26-

## 1. WHAT IS CLAIMED IS:

1. A diffractive subtractive color filter (Fig. 1) responsive to incident polychromatic illuminating light (118) having a given wavelength spectrum (a) for deriving reflection spectra (i) which vary as a function of the angle of incidence  $\alpha$  of said illuminating light and (ii) in which for each angle of incidence the reflection spectrum comprises separate portions that are polarized respectively parallel to and perpendicular to a given direction, and (b) for also deriving transmission spectra which are substantially the complement of said reflection spectra;

characterized by:

15 a first optical medium (100) having a thickness  $t$  between two opposite faces (102, 104) thereof, said first optical medium having a varying index-of-refraction which divides said first optical medium into juxtaposed periodic diffraction elements (106) of a diffractive structure having a period  $d$  which extends in a direction substantially parallel to said faces and perpendicular to said given direction, so that each one of said diffraction elements extends along a direction substantially parallel to said faces and parallel to said given direction,

25 the spatial distribution of said varying index-of-refraction within the volume of each diffraction element dividing that diffraction element into a plurality of separate three-dimensional regions (108, 110, 112) of certain-valued relatively higher and relatively lower indices-of-refraction, each of said regions having a specified size and shape, whereby the entire volume of each diffraction element has an average index-of-refraction  $\bar{n}$ ,

35 said average index-of-refraction  $\bar{n}$  being larger than the index-of-refraction  $n_2$  of a second optical medium (114) contacting one of said opposite faces and also larger than the index-of-refraction  $n_3$  of a third optical medium (116) contacting the other of said opposite faces, and



-27-

1 at all free space wavelengths  $\lambda$  within a  
sub-interval of said illuminating wavelength spectrum  
extending from a minimum wavelength  $\lambda_1$  up to a maximum  
wavelength  $\lambda_2$ , the following relationships are true

5

$$\bar{n} > \max(n_2, n_3) \quad (1)$$

$$d \max(n_2, n_3) < \lambda_2 \quad (2)$$

$$d(\bar{n} + 1) > \lambda_1 \quad (3)$$

10

$$4 \bar{n} t \geq \lambda_1 \quad (4)$$

15

where  $\max(n_2, n_3)$  is generally the larger of  $n_2$  and  $n_3$ ,  
but in the special case where  $n_2 = n_3$ , is  $n_2$  or  $n_3$ ,  
whereby the characteristics of each of said spectra  
depends on (1) the angle of incidence of said illuminating  
light, (2) the specified size and shape of each of said  
regions of said certain-valued relatively higher and  
relatively lower indices-of-refraction, so that the value  
20 of  $\bar{n}$  is determined, and (3) the respective physical values  
of  $d$  and  $t$ .

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-28-

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2. The diffractive subtractive color filter defined in claim 1, wherein at least the free space wavelengths of said sub-interval of the wavelength spectrum of said polychromatic illuminating light includes free space wavelengths within the range of 0.4-0.7 micrometer of visible light.

5

3. The diffractive subtractive color filter defined in claim 1 or 2,

10

wherein the angle  $\alpha$  is any angle between  $0^\circ$  and  $90^\circ$  in a plane normal to said faces and parallel to said given direction.

15

4. The diffractive subtractive color filter (e.g., Fig. 2) defined in claim 1, further including said second optical medium (114) and said third optical medium (116),

wherein said second optical medium is comprised of a solid material laminated to said one of said opposite faces (102) of said first medium,

20

wherein said third optical medium is comprised of a solid material laminated to said other of said opposite faces (104) of said first medium, and

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wherein the index-of-refraction  $n_2$  (1.5) of the solid material of which said second optical medium is composed and the index-of-refraction  $n_3$  (1.5) of the solid material of which said third optical medium is composed are both larger than unity.

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-29-

1           5. The diffractive subtractive color filter  
(Figs. 3, 3a, etc.) defined in claim 4,  
          wherein each diffractive element of said first  
          optical medium includes at least one first region (306)  
5           comprised of a solid material having an  
          index-of-refraction  $n_1$  larger than either  $n_2$  or  $n_3$ , at  
          least one second region contacting said second optical  
          medium (308) that is composed of the same solid material  
          as said second optical medium, and at least one third  
10          region contacting said third optical medium (304) that is  
          composed of the same solid material as said third optical  
          medium.

15          6. The diffractive subtractive color filter  
          defined in claim 5, wherein said second and third optical  
          mediums are composed of the same solid material, whereby  
           $n_2$  is equal to  $n_3$ .

20          7. The diffractive subtractive color filter  
          defined in claim 5, wherein said first region (306)  
          contacts both said second region and said third region.

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-30-

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8. The diffractive subtractive color filter (Figs. 3, 5, 7) defined in claim 7, wherein said second region contacts said third region.

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9. The diffractive subtractive color filter defined in claim 8, wherein said second and third optical mediums are composed of the same solid material, whereby  $n_2$  is equal to  $n_3$ .

10.

10. The diffractive subtractive color filter (Figs. 3a, 4) defined in claim 7, wherein said first region is situated in between said second and third regions and completely separates said second region from said third region so that there is no contact between said second and third regions.

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-31-

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11. The diffractive subtractive color filter (Fig. 3) defined in claim 5, wherein said third optical medium (304) and all third regions of said first optical medium (306) are comprised of a diffraction grating formed by a given periodic waveform having said period  $d$  and a given amplitude  $a$  embossed as a surface relief pattern in a solid material having said index-of-refraction  $n_3$ ,

10

wherein all said first regions of said first optical medium are comprised of solid material having said index-of-refraction  $n_1$  deposited on at least a portion of said surface relief pattern, said deposited material having predetermined thickness and shape characteristics, and

15

wherein said second optical medium and all said second regions of said first optical medium are comprised of an overcoat of solid material having said index-of-refraction  $n_2$  which covers said surface relief pattern and said deposited material, said overcoat filling in all those portions of said first optical medium not occupied by said first and third regions.

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-32-

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12. The diffractive subtractive color filter defined in claim 11, wherein the ratio of the index-of-refraction  $n_1$  to the larger of the indices-of-refraction  $n_2$  and  $n_3$  is at least 1.5.

13. The diffractive subtractive color filter defined in claim 11, wherein both the indices-of-refraction of  $n_2$  and  $n_3$  have a value of substantially 1.5,

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wherein the index-of-refraction of  $n_1$  has a value in the range of 1.7-5,

15

wherein the period  $d$  of said periodic waveform has a value in the range of 0.1-0.45 micrometer, wherein the amplitude  $a$  of such periodic waveform has a value in the range of 0.1-0.2 micrometer, and wherein the wavelength spectrum of said polychromatic illuminating light includes free space wavelengths within the range of 0.4-0.7 micrometer of visible light.

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-33-

1 14. The diffractive subtractive color filter  
defined in claim 11, wherein said periodic waveform of  
said diffraction grating is a rectangular waveform.

5 15. The diffractive subtractive color filter  
defined in claim 14, wherein said first regions are  
comprised of respective layers of said deposited material  
covering respectively the crests and the troughs of said  
rectangular waveform.

10 16. The diffractive subtractive color filter  
defined in claim 15, wherein said deposited layer-covering  
said crests and covering said troughs of said rectangular  
waveform both have substantially the same thickness  $c$ .

15 17. The diffractive subtractive color filter  
defined in claim 16, wherein the value of  $c$  is smaller  
than the value of  $a$ .

18. The diffractive subtractive color filter  
defined in claim 16, wherein the value of  $c$  is larger than  
the value of  $a$ .

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-34-

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19. The diffractive subtractive color filter defined in claim 15, wherein the deposited layer covering the troughs of said rectangular waveform has a thickness which is larger than the thickness of the deposited layer covering said crests but is smaller than the sum of the amplitude  $a$  of said rectangular waveform and the thickness of the deposited layer covering the crests of said rectangular waveform.

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20. The subtractive diffractive color filter (Fig. 5) defined in claim 14, wherein said first regions are comprised of L-shaped layers of said deposited material that cover the crests and a certain one of the two sides of said rectangular waveform, the deposited layers covering said crests and covering said certain one of the two sides of said rectangular waveform having respective thicknesses.

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-35-

1            21. The subtractive diffractive color filter (Fig. 7) defined in claim 11, wherein said predetermined waveform of said diffraction grating is a triangular waveform.

5            22. The diffractive subtractive color filter defined in claim 20, wherein said first regions are comprised of layers of deposited material covering a certain one of the sides of said triangular waveform.

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-36-

1                   23. method for utilizing a diffractive  
 subtractive filter comprising a first optical medium  
 having a thickness  $t$  between two opposite faces thereof,  
 said first optical medium having a varying  
 5                   index-of-refraction which divides said first optical  
 medium into juxtaposed periodic diffraction elements of a  
 diffractive structure having a period  $d$  which extends in a  
 direction substantially parallel to said faces and  
 perpendicular to a given direction, so that each one of  
 10                  said diffraction elements extends along a direction  
 substantially parallel to said faces and parallel to said  
 given direction, the spatial distribution of said varying  
 index-of-refraction within the volume of each diffraction  
 element dividing that diffraction element into a plurality  
 15                  of separate three-dimensional regions of certain-valued  
 relatively higher and relatively lower  
 indices-of-refraction, each of said regions having a  
 specified size and shape, whereby the entire volume of  
 each diffraction element has an average  
 20                  index-of-refraction  $\bar{n}$ , said average index-of-refraction  $\bar{n}$   
 being larger than the index-of-refraction  $n_2$  of a second  
 optical medium contacting one of said opposite faces and  
 also larger than the index-of-refraction  $n_3$  of a third  
 optical medium contacting the other of said opposite  
 25                  faces, and at all free space wavelengths  $\lambda$  within at least  
 a sub-interval extending from a minimum wavelength  $\lambda_1$  up  
 to a maximum wavelength  $\lambda_2$ , the following relationships  
 are true for all angles of incidence of illuminating light  
 in a range between zero and  $\alpha$  with respect to a plane  
 30                  normal to said faces and parallel to said given direction:

$$\bar{n} > \max(n_2, n_3) \quad (1)$$

$$d \max(n_2, n_3) < \lambda_2 \quad (2)$$

$$d(\bar{n} + 1) > \lambda_1 \quad (3)$$

$$4 \bar{n} t \geq \lambda_1 \quad (4)$$



-37-

1 where  $\max(n_2, n_3)$  is generally the larger of  $n_2$  and  $n_3$ ,  
but, in the special case where  $n_2 = n_3$ , is  $n_2$  or  $n_3$ ;  
said method including the steps of:

5 (a) illuminating said filter with diffuse  
polychromatic visible light which includes said  
wavelengths extending from  $\lambda_1 < \lambda < \lambda_2$  of said  
sub-interval;

10 (b) viewing a first color hue of the light  
reflected from said filter at a first given value of angle  
 $\alpha_1$  in a range between zero and  $\alpha$ , and

15 (c) viewing a second color hue different from  
said first color hue of the light reflected from said  
filter at a second given value of angle  $\alpha_2$  in said range  
between zero and  $\alpha$  which is different from said first  
given value of angle  $\alpha_1$ .

24. The method defined in claim 23, wherein  $\alpha$   
has a value of  $90^\circ$ , and

20 wherein step (b) comprises the step of viewing  
said first color hue at a first given value of angle  $\alpha_1$  in  
a range between  $0^\circ$  and  $90^\circ$ , and step (c) comprises the  
step of viewing said second color hue at a second given  
value of angle  $\alpha_2$  in said range between  $0^\circ$  and  $90^\circ$ .

25 25. The method defined in claim 23 or 24,  
wherein step (a) comprises illuminating said  
filter with diffuse white light having a wavelength  
spectrum extending from 0.4-0.7 micrometer.

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-38-

1           26. An article (Fig. 8) comprising an  
authenticated item of sheet material which is subject to  
counterfeiting and an authenticating device (800) bonded  
to said item, characterized in that said device includes  
5           (as, for the example, Fig. 3):

10           a substrate (304) bonded to said sheet material,  
said substrate being composed of a material having an  
index-of-refraction  $n_3$ , said substrate having a  
diffractive structure including at least one diffraction  
15           grating embossed as a surface relief pattern on an area of  
the viewable surface of said substrate, each diffraction  
grating having a line direction formed by a given periodic  
waveform having a period  $d$  perpendicular to said line  
direction and a given amplitude  $a$  embossed in said  
viewable surface,

20           a solid material (306) having an  
index-of-refraction  $n_1$  larger than  $n_3$  deposited on at  
least a given portion of each period of each embossed  
diffractive grating, said deposited material on said given  
portion of each period having the same predetermined  
25           thickness and shape characteristics such that a maximum  
overall thickness of size  $t$  of such diffraction grating in  
a direction normal to said viewable surface is formed by  
the sum of the amplitude  $a$  of that embossed diffraction  
grating and the thickness of said deposited material of  
that diffraction grating, and

30           an overcoat (308) composed of a solid material  
having an index-of-refraction  $n_2$  smaller than  $n_1$  which  
covers said relief pattern and said deposited material,  
said overcoat filling in all of the space within said  
overall thickness  $t$  of each diffraction grating not  
already occupied by said substrate material or by said  
deposited material,

35           wherein at all free space wavelengths  $\lambda$  within a  
sub-interval extending from a minimum wavelength  $\lambda_1$  up to  
a maximum wavelength  $\lambda_2$  of illuminating light, the  
following relationships are true for all angles of  
incidence of said illuminating light in a range between



-39-

1 zero and  $\alpha$  with respect to a plane normal to said variable  
surface and parallel to said line direction:

$$\bar{n} > \max(n_2, n_3) \quad (1)$$

$$5 d \max(n_2, n_3) < \lambda_2 \quad (2)$$

$$d(\bar{n} + 1) > \lambda_1 \quad (3)$$

$$4 \bar{n} t \geq \lambda_1 \quad (4)$$

10 where  $\bar{n}$  is the average index-of-refraction of the  
substrate material, the deposited material and the  
overcoat material within the volume of the space occupied  
by the overall thickness  $t$  of each diffraction grating,  
15 and where  $\max(n_2, n_3)$  is generally the larger of  $n_2$  and  
 $n_3$ , but, in the special case where  $n_2 = n_3$ , is  $n_2$  or  $n_3$ ,  
whereby the polarization and color  
characteristics of the spectra of the reflected light from  
each diffraction grating of said authenticating device  
20 viewed at a viewing angle between zero and  $\alpha$  is determined  
by the value of the viewing angle and by the set of  
parameters including (1) the values of the  
indices-of-refraction  $n_1$ ,  $n_2$  and  $n_3$ , (2) the given  
waveform of that diffraction grating (3) the predetermined  
25 thickness and shape characteristics of the deposited  
material of that diffraction grating and (4) the  
respective physical values of the period  $d$ , the amplitude  
 $a$  and the overall thickness  $t$  of that diffraction grating.

27. The article defined in claim 26,  
30 wherein the value of  $\alpha$  is  $90^\circ$ .



-40-

1           28. The article defined in claim 26,  
          wherein said diffractive structure (Fig. 9)  
          includes a first of said diffraction gratings (900)  
          occupying a first portion of the area of said diffractive  
5           structure and a second of said diffraction gratings (902)  
          occupying a second portion of the area of said diffractive  
          structure, and

10           wherein at least one of said parameters of said  
          first of said diffraction gratings is substantially  
          different from that of said second of said diffraction  
          gratings thereby to provide substantially different  
          polarization and color characteristics of the spectra of  
          the reflected light from said first and second diffraction  
          gratings for all viewing angles between zero and  $\alpha$ .

15           29. The article defined in claim 28, wherein  
          said first and second portions of the area of said  
          diffractive structure are contiguous with one another.

20           30. The article defined in claim 29, wherein  
          said second portion of the area surrounds the first  
          portion of the area of said diffractive structure.

31. The article defined in anyone of claims 28,  
29, and 30, wherein said one parameter is the value of  $d$ .

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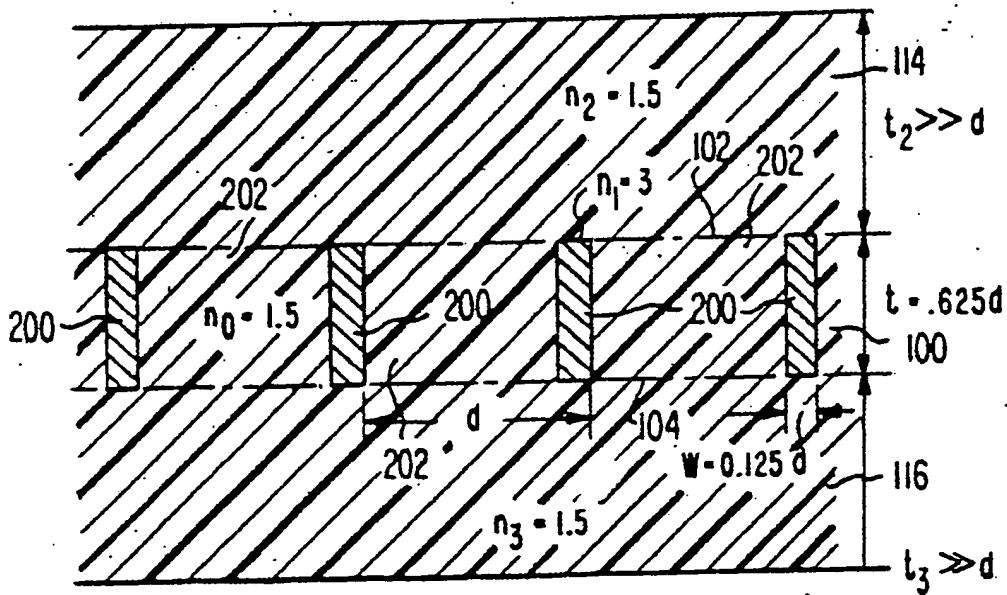
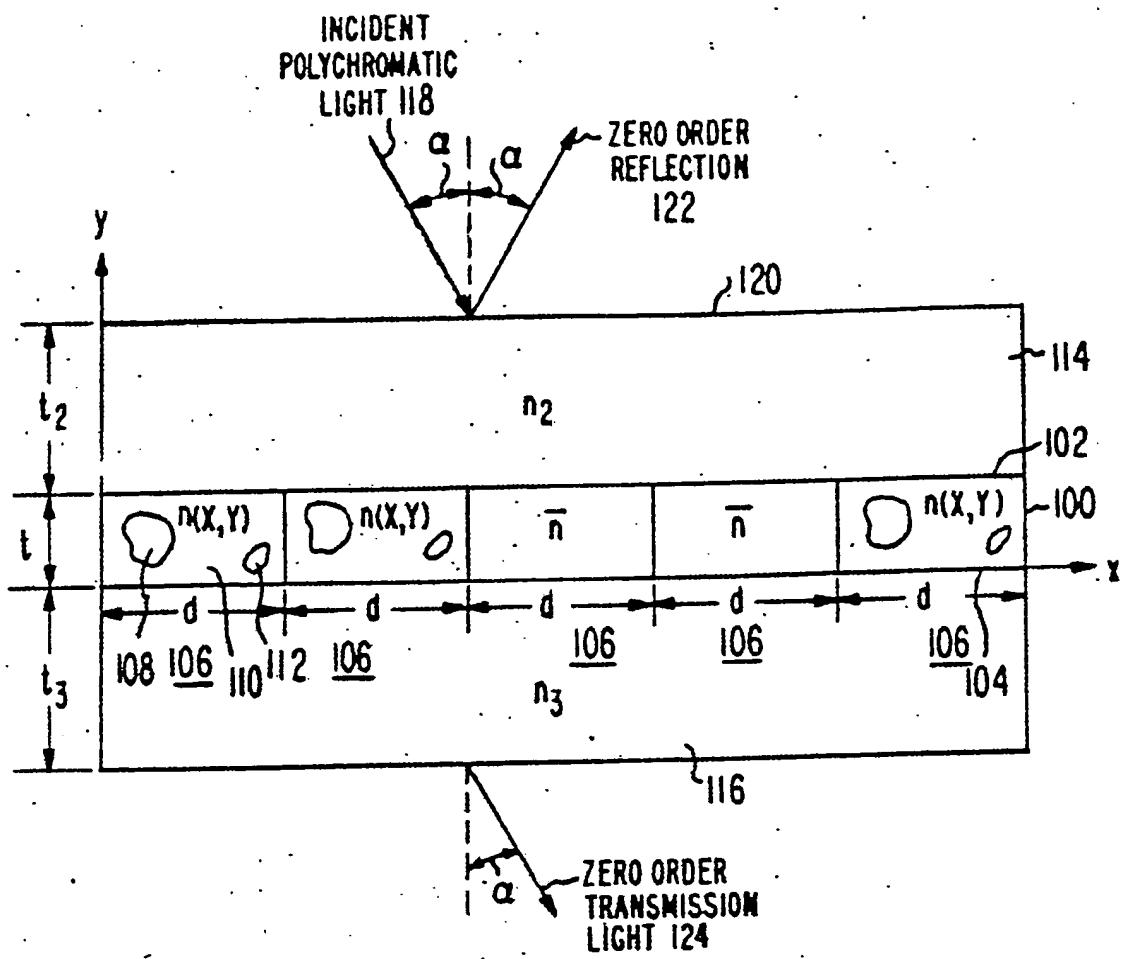


Fig. 2

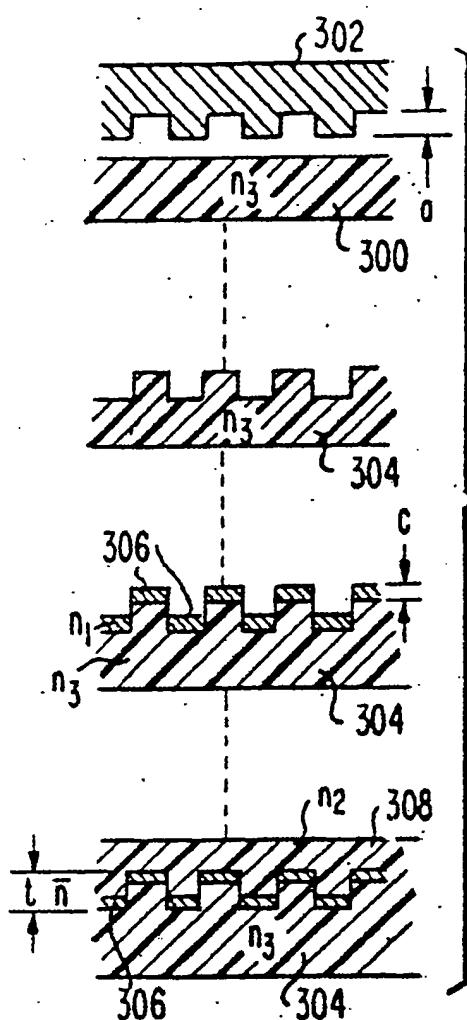


Fig. 3

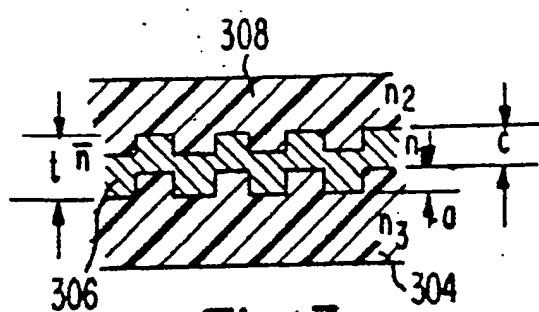


Fig. 3a

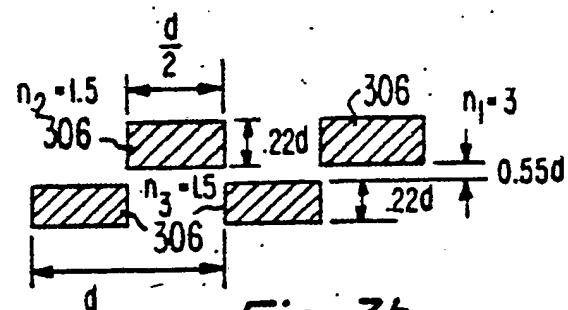


Fig. 3b

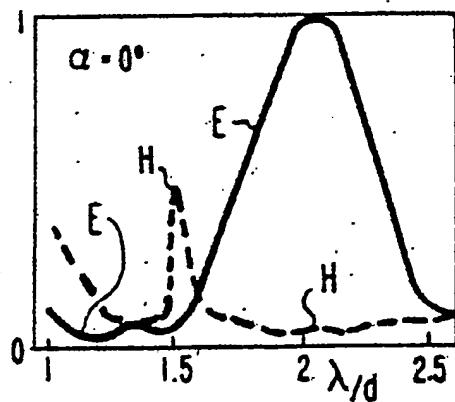


Fig. 3c

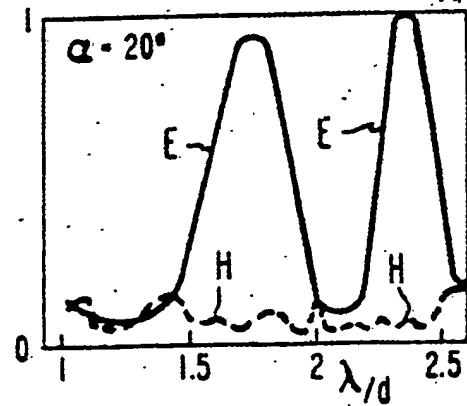


Fig. 3d

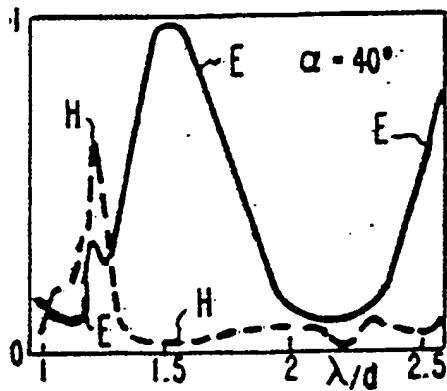


Fig. 3e

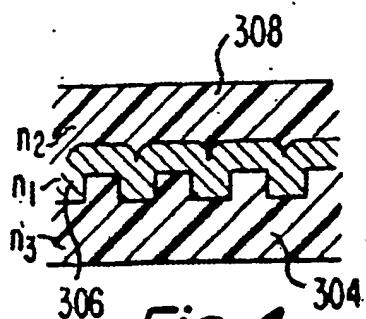


Fig. 4

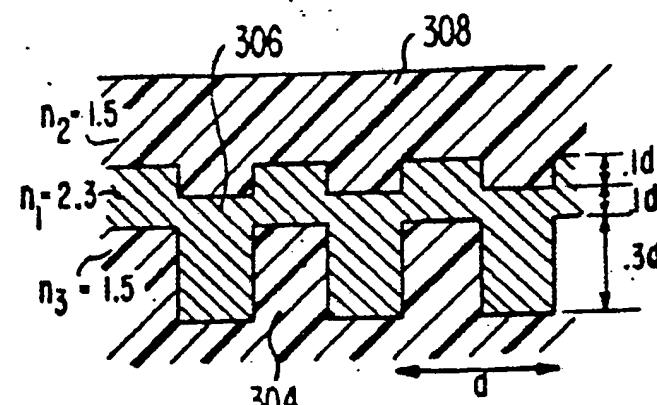


Fig. 4a

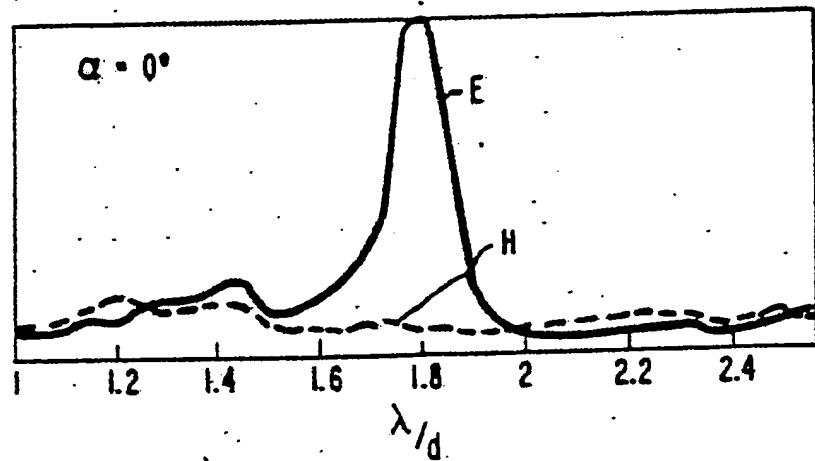


Fig. 4b

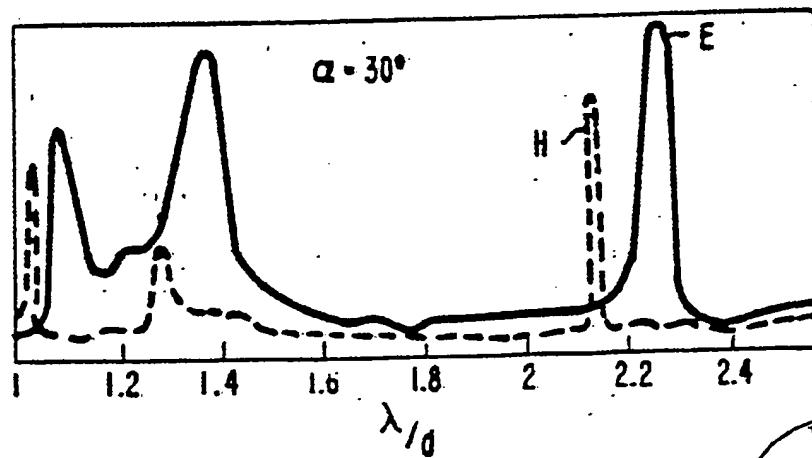


Fig. 4c

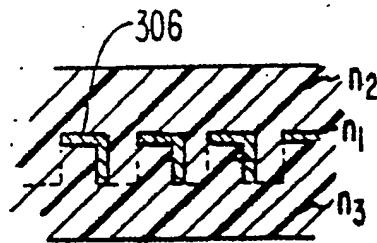


Fig. 5

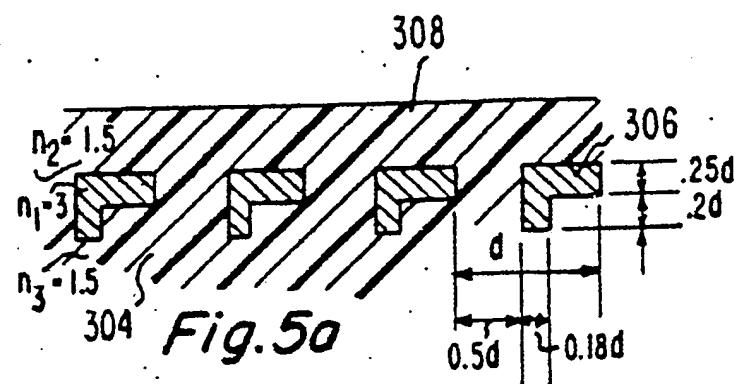


Fig. 5a

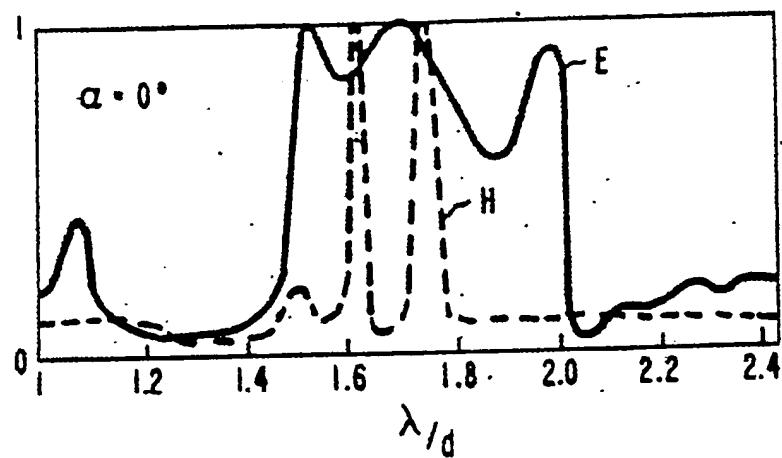


Fig. 5b

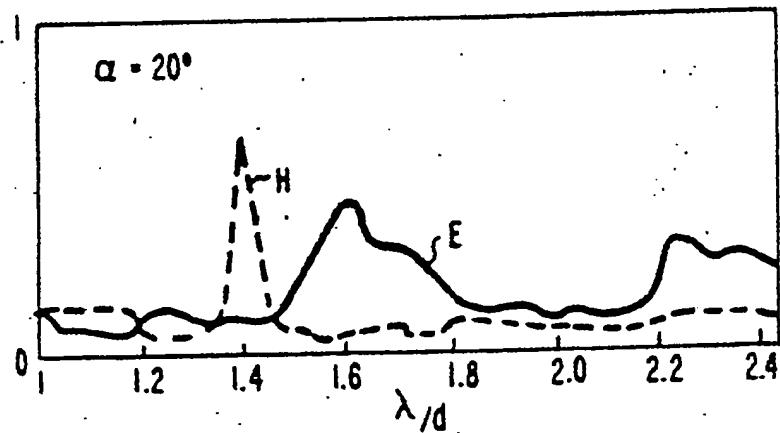


Fig. 5c

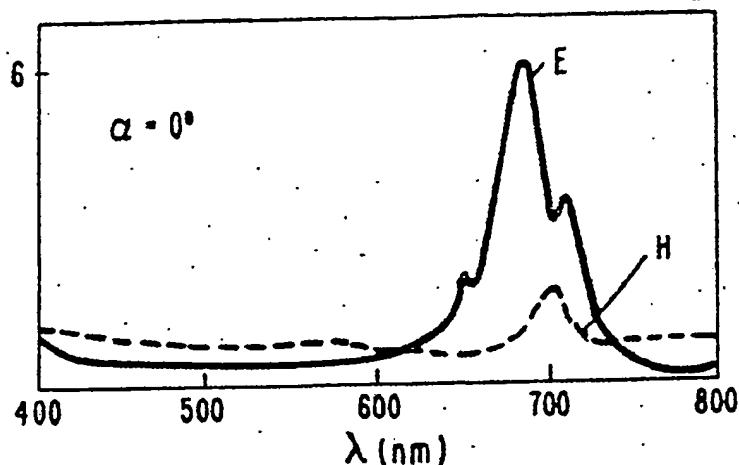


Fig. 6a

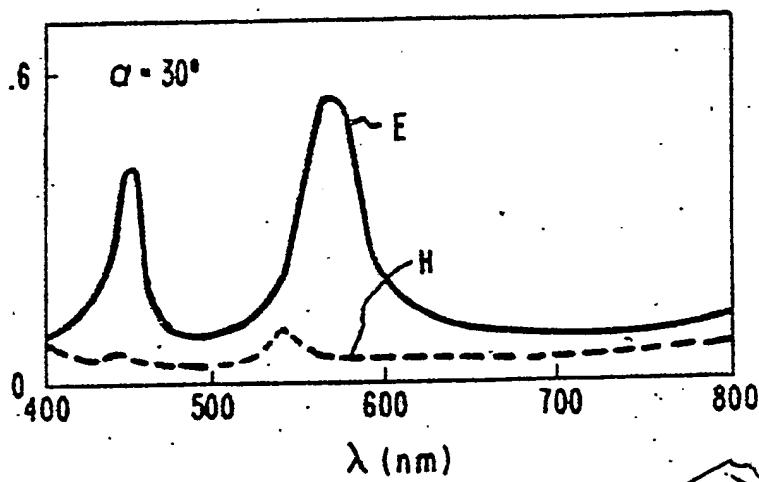


Fig. 6b

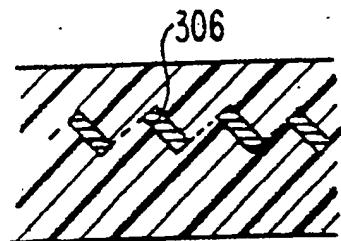


Fig. 7

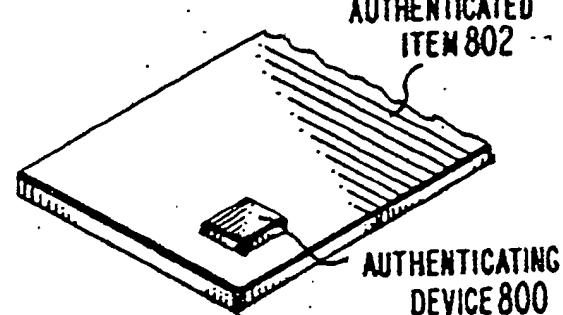


Fig. 8

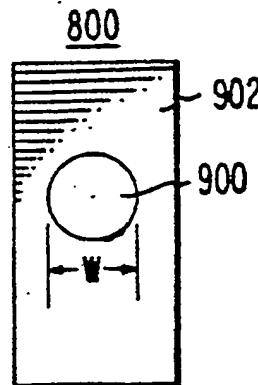


Fig. 9



## INTERNATIONAL SEARCH REPORT

International Application No. PCT/US82/00381

I. CLASSIFICATION OF SUBJECT MATTER (If several classification symbols are used, indicate all)<sup>1</sup>

According to International Patent Classification (IPC) or to both National Classification and IPC  
 INT. CL. 3 G02B 27/44  
 U.S. CL. 350/162R

## II. FIELDS SEARCHED

Minimum Documentation Searched<sup>4</sup>

Classification System	Classification Symbols
U.S.	350/162R, 162SF, 166

Documentation Searched other than Minimum Documentation  
to the Extent that such Documents are Included in the Fields Searched<sup>4</sup>

III. DOCUMENTS CONSIDERED TO BE RELEVANT<sup>1,4</sup>

Category <sup>5</sup>	Citation of Document, <sup>1,6</sup> with indication, where appropriate, of the relevant passages <sup>1,7</sup>	Relevant to Claim No. <sup>1,8</sup>
Y	US, A, 4,130,347, Published 19 December 1978	1-31
Y	US, A, 4,155,627, Published 22 May 1979	1-31
Y	US, A, 4,057,326, Published 08 November 1977	1-31
Y	US, A, 4,029,394, Published 14 June 1977	1-31
Y	US, A, 4,277,138, Published 07 July 1981	1-31
Y	US, A, 3,542,453, Published 24 November 1970	22
Y	US, A, 3,858,977, Published 07 January 1975	26-31
A	US, A, 3,957,354, Published 18 May 1976	
A	US, A, 3,759,604, Published 18 September 1973	
A	US, A, 4,255,019, Published 10 March 1981	
A	US, A, 3,911,479, Published 07 October 1975	

\* Special categories of cited documents:<sup>1,9</sup>

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"&" document member of the same patent family

## IV. CERTIFICATION

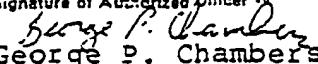
Date of the Actual Completion of the International Search<sup>2</sup>Date of Mailing of this International Search Report<sup>3</sup>

19 August 1982

03 SEP 1982

International Searching Authority<sup>4</sup>Signature of Authorized Officer<sup>10</sup>

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